

Quantum information science

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Lecture notes for the class during the 2nd trimester of the 2014/2015 school year.

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